

DEPARTMENT OF MATHEMATICS AND COMPUTER SCIENCE  
UNIVERSITY OF SOUTHERN DENMARK, ODENSE

## Mathematics seminar

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### Localizing gauge theories from noncommutative geometry

Thursday 3 November 2016, 14:15-15:15  
IMADA seminar room

#### Abstract

We review the emergence of a generalized gauge theory from a noncommutative Riemannian spin manifold, viz. a real spectral triple  $(A, H, D; J)$ . This includes a gauge group determined by the unitaries in the  $*$ -algebra  $A$ . Our main new result is the interpretation of this generalized gauge theory in terms of an upper semi-continuous  $C^*$ -bundle on a (Hausdorff) base space  $X$ . The gauge group acts by vertical automorphisms on this  $C^*$ -bundle and can (under some mild conditions) be identified with the space of continuous sections of a group bundle on  $X$ . This then allows for a geometrical description of the group of inner automorphisms of  $A$ . We exemplify our construction by Yang-Mills theory and toric noncommutative manifolds and show that they actually give rise to continuous  $C^*$ -bundles, which we explicitly determine.