DEPARTMENT OF MATHEMATICS AND COMPUTER SCIENCE UNIVERSITY OF SOUTHERN DENMARK, ODENSE

Mathematics seminar

Anders Yeo Singapore University of Technology and Design

Connections between graph theory, transversals in hypergraphs and Algorithms

Monday 7 December 2015, 12:15-13:15 IMADA seminar room

Abstract

We will first show the connection between total domination in graphs and transversals in hypergraphs. A set, S, of vertices in a graph, G, is a total dominating set if and only if every vertex of G has a neighbour in S. A hypergraph is a generalization of a graph, in the sense that hyperedges can contain any number of vertices and not just two as in a graph. A transversal in a hypergraph is a set of vertices intersecting every hyperedge.

We will give a short survey of results on transversals in hypergraphs together with some applications. For example, we will mention a recent (unpublished) proof of the well-known Tuza-Vestergaard conjecture.

* Tuza-Vestergaard Conjecture: If every hyperedge in a hypergraph, H, contains 6 vertices and every vertex belongs to 3 hyperedges, then one can always find a transversal containing at most a quater of the vertices in H.

We will furthermore briefly explain the notion of a fixed parameter tractable algorithm and relate this to the above.

During the presentation we will use and relate the results to other areas of directed and undirected graph theory.