## Adaptive harvest under invasive Induced mortality

Jon Olaf Olaussen* ,Yajie Liu**, Anders Skonhoft ${ }^{* * *}$
*Trondheim Business School
**Sintef Fisheries \& Aquaculture
***Department of Economics, NTNU

## Wild salmon: Ecological problems

■ Farmed salmon: Cross breeding (hybrids)
$\square$ Genetic pollution
$\square$ Destroying spawning nests

- Spread of deceases
$\square$ Furunculosis
$\square$ Gyrodactylus salaris
- Farmed salmon: Salmon lice (Lepeophtheirus)


## Recent years:

- Salmon lice density
- Increased by aquaculture
$\square$ Heuch et al 2005
- Smolt on out-migration journey
$\square$ Have to pass fish farms
- More than 10 salmon lice per smolt: certain death
$\square$ Revie et al 2009


## Invasive?

- Salmon lice
$\square$ Native
- Dominant colonization of habitat
$\square$ Due to human action (fish farming)
$\square$ Disturbing the balance of species


## Main solutions:

1. Farming sector: Reduce sea lice density in fish farms?
$\square$ Resistance to treatment
2. Wild sector: Reduce fishing mortality?
3. Wild sector: Change harvesting pattern?




## The model

- Three mature age classes:
- 1 Sea-winter (1SW)
$\square<3 k g$
- 2 Sea-winter (2SW)
$\square 3-7 \mathrm{~kg}$
- 3 Sea-winter (3SW)
$\square>7 \mathrm{~kg}$


## Why age class model?

- Previous management: Uniform harvest rate across stages ("a salmon is a salmon")
- Recent management trend: Stage specific harvest
$\square$ Catch and release
$\square$ «No take» of 2 and 3 SW
$\square$ Bag limits for 1, 2 and 3SW


## Anectodical background

- Salmon anglers want to kill "all" 1SW salmon
- Common view:
$\square 1$ SW salmon does not contribute to spawning (about $80 \%$ is male)
$\square$ Should harvest most 1SW, less 2SW and even less 3SW
- Will the model confirm?


## The overall aim

- Look at different harvest regimes for wild salmon
- Uniform harvest rate versus stage specific harvest rate
- Stage specific harvest rates versus fixed uniform harvest rates
- Harvest (use) values versus non-use values


## Lagrangian

$$
\begin{aligned}
& L=\left[p_{4} w_{4} s_{3} \sigma f_{4}+p_{5} w_{5} s_{3}(1-\sigma) \varphi s_{4} f_{5}+p_{6} w_{6} s_{3}(1-\sigma-\varphi+\varphi \sigma) s_{4} s_{5} f_{6}\right] N_{3} \\
& -\lambda\left[N_{3}-s R(B)\right] \\
& -\mu\left\{B-\left[\gamma_{4} s_{3} \sigma\left(1-f_{4}\right)+\gamma_{5} s_{3}(1-\sigma) \varphi s_{4}\left(1-f_{5}\right)+\gamma_{6} s_{3}(1-\sigma-\varphi+\varphi \sigma) s_{4} s_{5}\left(1-f_{6}\right)\right] N_{3}\right\}
\end{aligned}
$$

## FOC:

$$
\begin{array}{ll}
\partial L / \partial f_{4}=N_{3}\left(p_{4} w_{4}-\mu \gamma_{4}\right) \frac{\geq}{<} 0 & 0 \leq f_{4} \leq 1 \\
\partial L / \partial f_{5}=N_{3}\left(p_{5} w_{5}-\mu \gamma_{5}\right) & (1 S W)  \tag{2SW}\\
<0 & 0 \leq f_{5} \leq 1
\end{array}
$$

- Biomass-value $\left(p_{i} w_{i}\right)$ - fecundity $\left(y_{i}\right)$ ratio

$$
p_{i} w_{i} / \gamma_{i}
$$

$$
i=4,5,6
$$

## Norwegian salmon data give:

$$
p_{4} w_{4} / \gamma_{4}>p_{6} w_{6} / \gamma_{6}>p_{5} w_{5} / \gamma_{5}
$$

## Possible harvest patterns:

vi) $f_{4}=1, f_{6}=1,0<f_{5}<1$
vii) $f_{4}=1, f_{6}=1, f_{5}=0$
viii) $f_{4}=1,0<f_{6}<1, f_{5}=0$
ix) $f_{4}=1, f_{6}=0, f_{5}=0$
x) $0<f_{4}<1, f_{6}=0, f_{5}=0$

Table 2: Optimal fishing mortalities under different sea lice induced mortality levels

|  | $f_{4}$ | $\boldsymbol{f}_{5}$ | $f_{6}$ | $N_{3}$ | $\mathbf{B}$ | $\mathbf{H}_{\mathbf{4}}$ | $\mathbf{H}_{\mathbf{5}}$ | $\mathbf{H}_{6}$ | $\boldsymbol{\pi}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Baseline | 1 | 0.52 | 1 | 1663 | 494 | 358 | 68 | 53 | $\mathbf{5 , 5 1 7}$ |
| $\mathbf{s = 0 . 0 4}$ | 1 | 0.46 | 1 | 1299 | 431 | 279 | 47 | 41 | $\mathbf{4 , 2 0 6}$ |
| $\mathbf{s}=\mathbf{0 . 0 3}$ | 1 | 0.38 | 1 | 933 | 359 | 202 | 28 | 30 | $\mathbf{2 , 9 3 2}$ |
| $\mathbf{s}=\mathbf{0 . 0 2}$ | 1 | 0.24 | 1 | 587 | 275 | 126 | 11 | 19 | $\mathbf{1 , 7 1 8}$ |
| $\mathbf{s}=\mathbf{0 . 0 1}$ | 1 | 0 | 0.98 | 240 | 151 | 52 | 0 | 8 | $\mathbf{6 1 7}$ |
| $\mathbf{s = 0 . 0 0 5}$ | 1 | 0 | 0.30 | 90 | 79 | 19 | 0 | 1 | $\mathbf{1 7 0}$ |
| $\mathbf{s = 0 . 1}$ | $\mathbf{1}$ | $\mathbf{0 . 6 6}$ | $\mathbf{1}$ | $\mathbf{3 5 2 4}$ | $\mathbf{7 4 0}$ | $\mathbf{7 5 8}$ | $\mathbf{1 8 2}$ | $\mathbf{1 1 3}$ | $\mathbf{1 2 , 3 8 0}$ |

Note: $f_{4}, f_{5}$ and $f_{6}$ are harvest rates for the $1 \mathrm{SW}, 2 \mathrm{SW}$ and 3 SW class, respectively. $N_{3}$ is the potentially harvestable population while $B$ is the spawning population. $H_{4}, H_{5}$, and $H_{6}$ are the harvest (in number of salmon) of the $1 \mathrm{SW}, 2 \mathrm{SW}$, and 3 SW , respectively while $\pi$ is the yearly profit in NOK 1000. s is the lumped survival rate from the juvenile to the smolt stage.

Table 3: Optimal uniform fishing mortality under different sea lice induced mortality levels

|  | $f_{4}$ | $\boldsymbol{f}_{5}$ | $\boldsymbol{f}_{\mathbf{6}}$ | $N_{\mathbf{3}}$ | $\mathbf{B}$ | $\mathbf{H}_{\mathbf{4}}$ | $\mathbf{H}_{\mathbf{5}}$ | $\mathbf{H}_{\mathbf{6}}$ | $\boldsymbol{\pi}$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Baseline | 0.80 | 0.80 | 0.80 | 1593 | 391 | 273 | 99 | 41 | $\mathbf{5 , 0 5 8}$ |
| $\mathbf{s = 0 . 0 4}$ | 0.77 | 0.77 | 0.77 | 1236 | 339 | 205 | 75 | 31 | $\mathbf{3 , 8 0 6}$ |
| $\mathbf{s = 0 . 0 3}$ | 0.74 | 0.74 | 0.74 | 884 | 280 | 140 | 51 | 21 | $\mathbf{2 , 6 0 0}$ |
| $\mathbf{s = 0 . 0 2}$ | 0.68 | 0.68 | 0.68 | 542 | 210 | 79 | 29 | 12 | $\mathbf{1 , 4 6 7}$ |
| $\mathbf{s = 0 . 0 1}$ | 0.54 | 0.54 | 0.54 | 218 | 120 | 26 | 9 | 4 | $\mathbf{4 7 4}$ |
| $\mathbf{s = 0 . 0 0 5}$ | 0.36 | 0.36 | 0.36 | 71 | 55 | 10 | 28 | 17 | $\mathbf{1 0 1}$ |
| $\mathbf{s = 0 . 1}$ | $\mathbf{0 . 8 6}$ | $\mathbf{0 . 8 6}$ | $\mathbf{0 . 8 6}$ | $\mathbf{3 4 2 4}$ | $\mathbf{5 9 4}$ | $\mathbf{6 3 0}$ | $\mathbf{2 2 9}$ | $\mathbf{9 4}$ | $\mathbf{1 1 , 6 9 0}$ |

Note: $f_{4}, f_{5}$ and $f_{6}$ are harvest rates for the 1SW, 2SW and 3SW class, respectively. $N_{3}$ is the potentially harvestable population while $B$ is the spawning population. $H_{4}, H_{5}$, and $H_{6}$ are the harvest (in number of salmon) of the $1 \mathrm{SW}, 2 \mathrm{SW}$, and 3 SW , respectively while $\pi$ is the yearly profit in NOK 1000. $s$ is the lumped survival rate from the juvenile to the smolt stage.

## Table 4: Fixed uniform fishing mortality under different sea lice induced mortality levels

|  | $\boldsymbol{f}_{4}$ | $f_{5}$ | $f_{6}$ | $N_{3}$ | $\mathbf{B}$ | $\mathbf{H}_{4}$ | $\mathbf{H}_{\mathbf{5}}$ | $\mathbf{H}_{\mathbf{6}}$ | $\boldsymbol{\pi}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Baseline | 0.80 | 0.80 | 0.80 | 1593 | 391 | 273 | 99 | 41 | $\mathbf{5 , 0 5 8}$ |
| $\mathbf{s = 0 . 0 4}$ | 0.80 | 0.80 | 0.80 | 1193 | 294 | 204 | 74 | 30 | $\mathbf{3 , 7 8 8}$ |
| $\mathbf{s = 0 . 0 3}$ | 0.80 | 0.80 | 0.80 | 793 | 195 | 136 | 50 | 20 | $\mathbf{2 , 5 2 0}$ |
| $\mathbf{s = 0 . 0 2}$ | 0.80 | 0.80 | 0.80 | 393 | 97 | 67 | 25 | 10 | $\mathbf{1 , 2 4 9}$ |
| $\mathbf{s = 0 . 0 1}$ | 0.80 | 0.80 | 0.80 | 0 | 0 | 0 | 0 | 0 | $\mathbf{0}$ |
| $\mathbf{s = 0 . 0 0 5}$ | 0.80 | 0.80 | 0.80 | 0 | 0 | 0 | 0 | 0 | $\mathbf{0}$ |
| $\mathbf{s = 0 . 1}$ | $\mathbf{0 . 8 0}$ | $\mathbf{0 . 8 0}$ | $\mathbf{0 . 8 0}$ | $\mathbf{3 5 9 3}$ | $\mathbf{8 8 4}$ | $\mathbf{6 1 5}$ | $\mathbf{2 2 4}$ | $\mathbf{9 2}$ | $\mathbf{1 1 , 4 1 0}$ |

Note: $f_{4}, f_{5}$ and $f_{6}$ are harvest rates for the $1 \mathrm{SW}, 2 \mathrm{SW}$ and 3 SW class, respectively. $N_{3}$ is the potentially harvestable population while $B$ is the spawning population. $H_{4}, H_{5}$, and $H_{6}$ are the harvest (in number of salmon) of the $1 \mathrm{SW}, 2 \mathrm{SW}$, and 3 SW , respectively while $\pi$ is the yearly profit in NOK 1000. $s$ is the lumped survival rate from the juvenile to the smolt stage.

## Conclusion 1:

- Stage specific versus optimal uniform harvest rate
$\square$ Profits increases by 9-70\%
- Stage specific versus fixed uniform harvest rate
$\square$ Fixed may lead to exctinction


## Management:

- Harvest 1SW, then 3SW and eventually 2SW
- Hence, general angler opinion:
$\square$ Correct with respect to 1SW
$\square$ Wrong with respect to 2 SW versus 3SW


## Extension: Adding non-use

 values- Maximizing social sustainable value: W
$\square$ Harvest value (Y) + Non-use value (Q)

$$
W=\alpha U(Y)+(1-\alpha) V(Q)
$$

- $U(Y)$ and $V(Q)$ both concave with $\alpha$ as the weighting factor
- Above results: $\alpha=1$

$$
\begin{aligned}
& L=\alpha\left[U\left(\left(z_{4} w_{4} s_{3} \sigma f_{4}+z_{3} w_{j} s_{3} s_{3}(1-\sigma) \varphi \varphi_{4} f_{5}+z_{6} w_{6} s_{3}(1-\sigma-\varphi+\varphi \sigma) s_{4} s_{5} f_{6}\right) N_{3}\right)\right] \\
& +(1-\alpha)\left[V\left(\left(w_{4} s_{3} \sigma\left(1-f_{4}\right)+w_{5} s_{3}(1-\sigma) \varphi s_{4}\left(1-f_{5}\right)+w_{6} s_{3}(1-\sigma-\varphi+\varphi \sigma) s_{4} s_{j}\left(1-f_{6}\right) N_{3}\right)\right]\right. \\
& -\lambda\left[N_{3}-s R(B)\right] \\
& -\mu\left\{B-\left[\gamma_{4} s_{j} \sigma\left(1-f_{4}\right)+\gamma_{5} s_{3}(1-\sigma) \varphi s_{4}\left(1-f_{5}\right)+\gamma_{6} s_{3}(1-\sigma-\varphi+\varphi \sigma) s_{4} s_{5}\left(1-f_{6}\right)\right] N_{3}\right\},
\end{aligned}
$$

(9') $\quad w_{4} / \gamma_{4} \frac{\geq}{<} \mu /\left[\alpha U^{\prime}(.) z_{4}-(1-\alpha) V^{\prime}().\right]$
$\left(10^{\prime}\right) w_{5} / \gamma_{5} \underset{<}{\underset{<}{2}} \mu /\left[\alpha U^{\prime}(.) z_{5}-(1-\alpha) V^{\prime}().\right]$
$\left(11^{\prime}\right) w_{6} / \gamma_{6} \frac{\geq}{<} \mu /\left[\alpha U^{\prime}(.) z_{6}-(1-\alpha) V^{\prime}().\right]$

Table 2: Managing for harvest value only $(\alpha=1)$. Optimal fishing mortalities under different sea lice-induced mortality levels.

|  | $f_{4}$ | $f_{5}$ | $f_{6}$ | $N_{3}$ | $H_{4}$ | $H_{5}$ | $H_{6}$ | $U$ | $V$ | $W$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathrm{~s}=0.05$ | 1 | 0.52 | 1 | 1,663 | 358 | 68 | 53 | 3.808 | 1.884 | 3.808 |
| $\mathrm{~s}=0.04$ | 1 | 0.46 | 1 | 1,299 | 279 | 47 | 42 | 3.535 | 1.755 | 3.535 |
| $\mathrm{~s}=0.03$ | 1 | 0.38 | 1 | 933 | 202 | 28 | 30 | 3.175 | 1.568 | 3.175 |
| $\mathrm{~s}=0.02$ | 1 | 0.24 | 1 | 587 | 126 | 11 | 19 | 2.641 | 1.301 | 2.641 |
| $\mathrm{~s}=0.01$ | 1 | 0 | 0.98 | 240 | 51 | 0 | 8 | 1.618 | 0.698 | 1.618 |
| $\mathrm{~s}=0.005$ | 1 | 0 | 0.30 | 90 | 19 | 0 | 1 | 0.282 | 0.088 | 0.282 |

Note: $s$ is the lumped survival rate from the juvenile to the smolt stage where $s=0.05$ is the survival rate in absence of sea lice. $f_{4}, f_{5}$ and $f_{6}$ are harvest rates for the $1 \mathrm{SW}, 2 \mathrm{SW}$ and 3 SW class, respectively. $N_{3}$ is the potentially harvestable population. $H_{4}, H_{5}$, and $H_{6}$ are the harvest (in number of salmon) of the 1 SW , 2 SW , and 3 SW , respectively, while $U$ is the utility in the recreational fishery, $V$ is the non-consumptive utility and $W$ is the weighted social welfare ( $\mathrm{U}, \mathrm{V}$ and W all measured in 100000 NOK ). $1 \mathrm{NOK}=0.17 \mathrm{USD}$ (Aug. 21 2013)

Table 3: Managing for harvest and non-consumptive values ( $\alpha=0.5$ ). Optimal fishing mortalities under different sea lice-induced mortality levels.

|  | $f_{4}$ | $f_{5}$ | $f_{6}$ | $N_{3}$ | $H_{4}$ | $H_{5}$ | $H_{6}$ | $U$ | $V$ | $W$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathrm{~s}=0.05$ | 1 | 0 | 0.31 | 1,886 | 405 | 0 | 19 | 3.372 | 3.148 | 3.260 |
| $\mathrm{~s}=0.04$ | 1 | 0 | 0.29 | 1,287 | 320 | 0 | 14 | 3.124 | 2.920 | 3.022 |
| $\mathrm{~s}=0.03$ | 1 | 0 | 0.25 | 1089 | 234 | 0 | 9 | 2.791 | 2.627 | 2.709 |
| $\mathrm{~s}=0.02$ | 1 | 0 | 0.17 | 692 | 149 | 0 | 4 | 2.292 | 2.211 | 2.252 |
| $\mathrm{~s}=0.01$ | 1 | 0 | 0 | 299 | 64 | 0 | 0 | 1.350 | 1.445 | 1.398 |
| $\mathrm{~s}=0.005$ | 0.94 | 0 | 0 | 100 | 20 | 0 | 0 | 0.195 | 0.391 | 0.293 |

Note: $f_{4}, f_{5}$ and $f_{6}$ are harvest rates for the $1 \mathrm{SW}, 2 \mathrm{SW}$ and 3 SW class, respectively. $N_{3}$ is the potentially harvestable population. $H_{4}, H_{5}$, and $H_{6}$ are the harvest (in number of salmon) of the 1 SW , 2 SW , and 3 SW , respectively, while $U$ is the utility in the recreational fishery, $V$ is the non-consumptive utility and $W$ is the weighted social welfare. $s$ is the lumped survival rate from the juvenile to the smolt stage where $s=0.05$ is the survival rate in absence of sea lice.

Table 6: Managing for harvest and non-consumptive values ( $\alpha=0.5$ ). Optimal uniform fishing mortality under different sea lice-induced mortality levels.

|  | $f_{4}$ | $f_{5}$ | $f_{6}$ | $N_{3}$ | $H_{4}$ | $H_{5}$ | $H_{6}$ | $U$ | $V$ | $W$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathrm{~s}=0.05$ | 0.46 | 0.46 | 0.46 | 1,846 | 183 | 67 | 27 | 3.322 | 3.152 | 3.237 |
| $\mathrm{~s}=0.04$ | 0.45 | 0.45 | 0.45 | 1,448 | 141 | 51 | 21 | 3.062 | 2.924 | 2.993 |
| $\mathrm{~s}=0.03$ | 0.44 | 0.44 | 0.74 | 1,052 | 99 | 36 | 15 | 2.711 | 2.630 | 2.670 |
| $\mathrm{~s}=0.02$ | 0.41 | 0.41 | 0.41 | 659 | 58 | 21 | 9 | 2.179 | 2.209 | 2.194 |
| $\mathrm{~s}=0.01$ | 0.34 | 0.34 | 0.34 | 274 | 20 | 7 | 3 | 1.115 | 1.443 | 1.279 |
| $\mathrm{~s}=0.005$ | 0.23 | 0.23 | 0.23 | 92 | 4 | 2 | 1 | 0.004 | 0.512 | 0.258 |

Note: $f_{4}, f_{5}$ and $f_{6}$ are harvest rates for the $1 \mathrm{SW}, 2 \mathrm{SW}$ and 3 SW class, respectively. $N_{3}$ is the potentially harvestable population. $H_{4}, H_{5}$, and $H_{6}$ are the harvest (in number of salmon) of the 1SW, 2SW, and $3 S W$, respectively, while $U$ is the utility in the recreational fishery, $V$ is the non-consumptive utility and $W$ is the weighted social welfare. $s$ is the lumped survival rate from the juvenile to the smolt stage where $s=0.05$ is the survival rate in absence of sea lice.

## Conclusion 2:

- Adding non-use values:
$\square$ Harvest pattern less aggressive
$\square$ Stage specific versus optimal uniform harvest rate
- Profits increases by 1-14\% (9-70\%)
- Stage structured harvest dampens effect of invasive induced mortality
$\square$ But less when non-use values are included

